



Recent Progress in the High-Gain FEL Theory

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Introduction

- A fourth-generation light source: a high-gain x-ray FEL operated in SASE mode
- 3D theory in the exponential growth regime well developed (energy spread, emittance, diffraction, guiding)
- Tremendous progress in high-gain experiments
wavelength down to < 100 nm
saturation achieved
- Stimulate better understandings of high-gain theory, some aspects are discussed in this talk
(mostly based on collaborative work with K.-J. Kim)



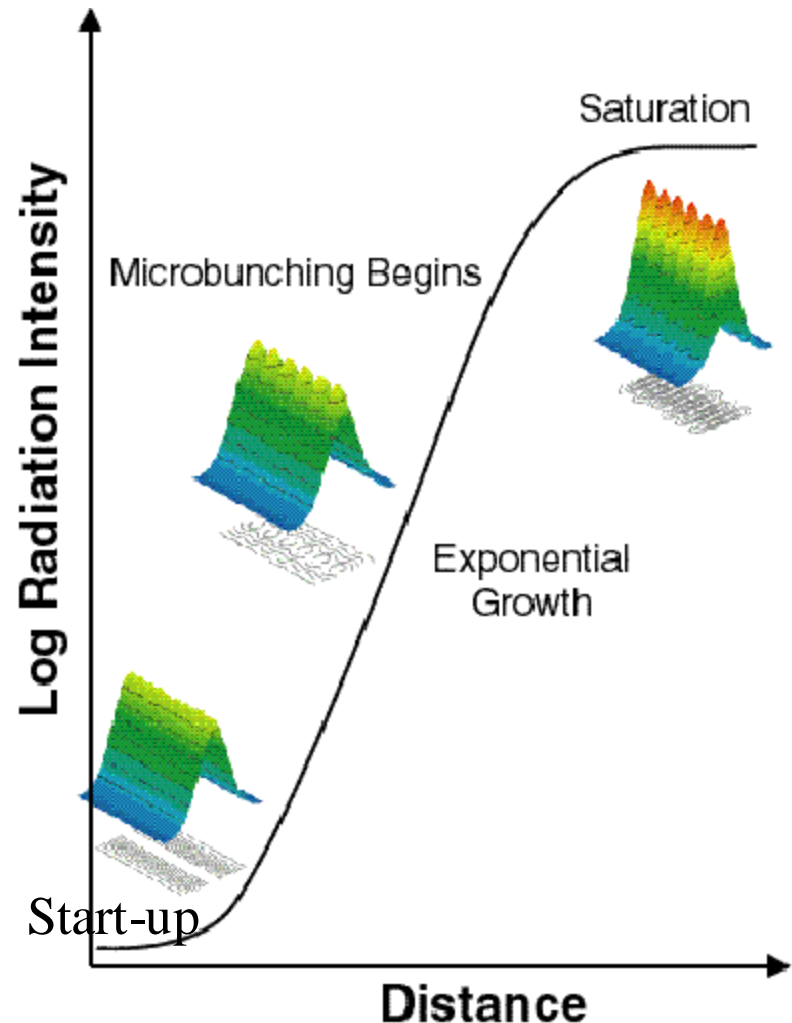
Theory: Overview

Start-up stage

External signal or spontaneous radiation interacts with the e-beam resonantly at undulator λ

Energy modulation \rightarrow density modulation (microbunching) \rightarrow coherent radiation at λ \rightarrow **exponential growth (L_G)**

At sufficiently high power, electrons fully microbunched and trapped in the ponderomotive field \rightarrow reach **saturation (P_{sat})**





Start-up Process

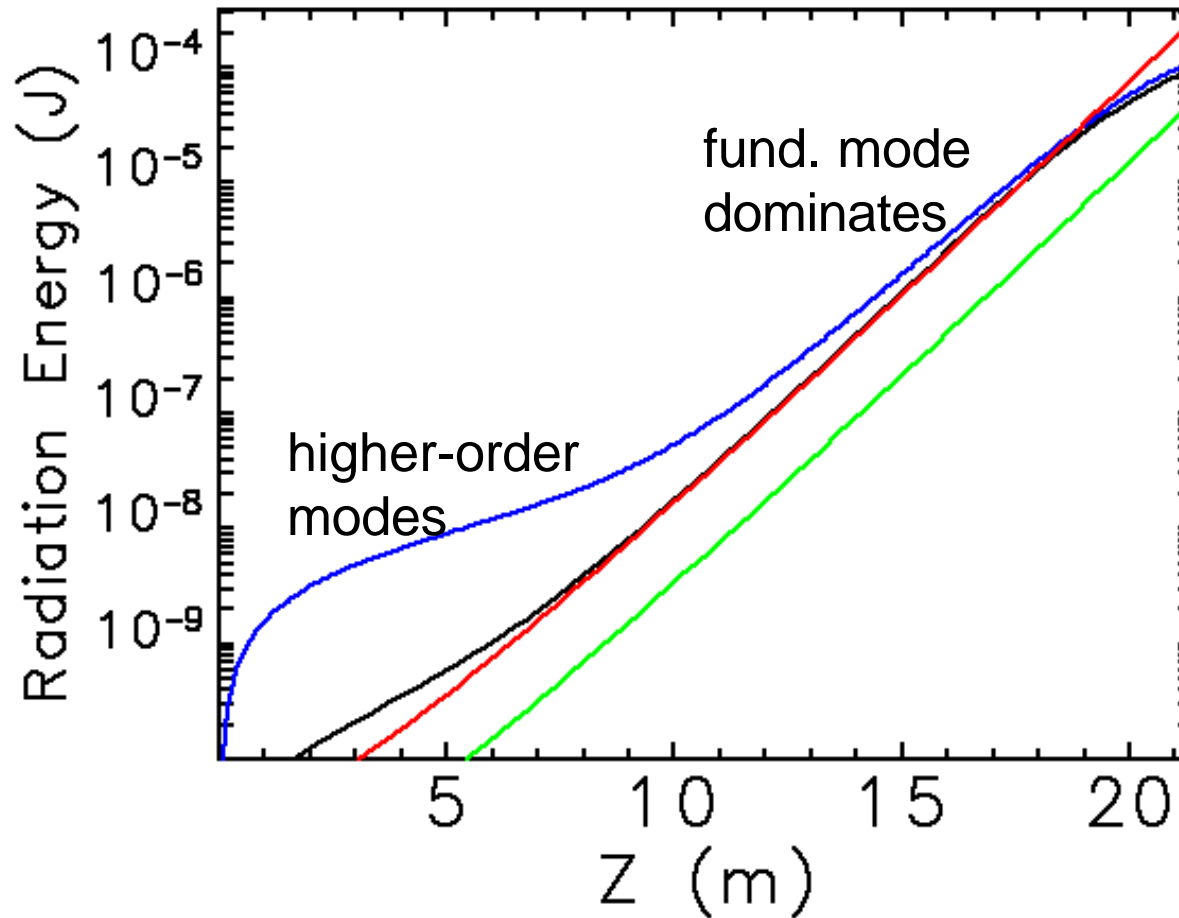
- Spontaneous emission: many transverse modes
- FEL instability favors a particular (fundamental) mode
- proper modal decomposition for initial value problem

$$\frac{dP}{d\mathbf{w}} = g_A \left[\left(\frac{dP}{d\mathbf{w}} \right)_{\text{signal}} + \left(\frac{dP}{d\mathbf{w}} \right)_{\text{noise}} \right] \exp \left(\frac{Z}{L_G} - \frac{(\Delta \mathbf{w})^2}{2\mathbf{S}_{\mathbf{w}}^2} \right)$$

- Effective start-up noise (for SASE): power of the fundamental mode over the first two gain length L_G , can increase with energy spread and emittance through L_G
- 2D Solution determines the radiation energy level in exponential gain regime



Comparison with Time-dependent Codes



GENESIS 3D

GINGER 2D

Theory 2D

Theory 1D*

* 2D L_G used



Transverse and Temporal Properties: Review

- Diffraction + Gain \rightarrow transverse mode selection
 - \Rightarrow fundamental mode dominates (gain guiding)
 - \Rightarrow good transverse coherence

- SASE is a chaotic light temporally

Coherence length = $(2\sigma_\omega)^{-1} (\propto \sqrt{z}) \ll$ bunch length

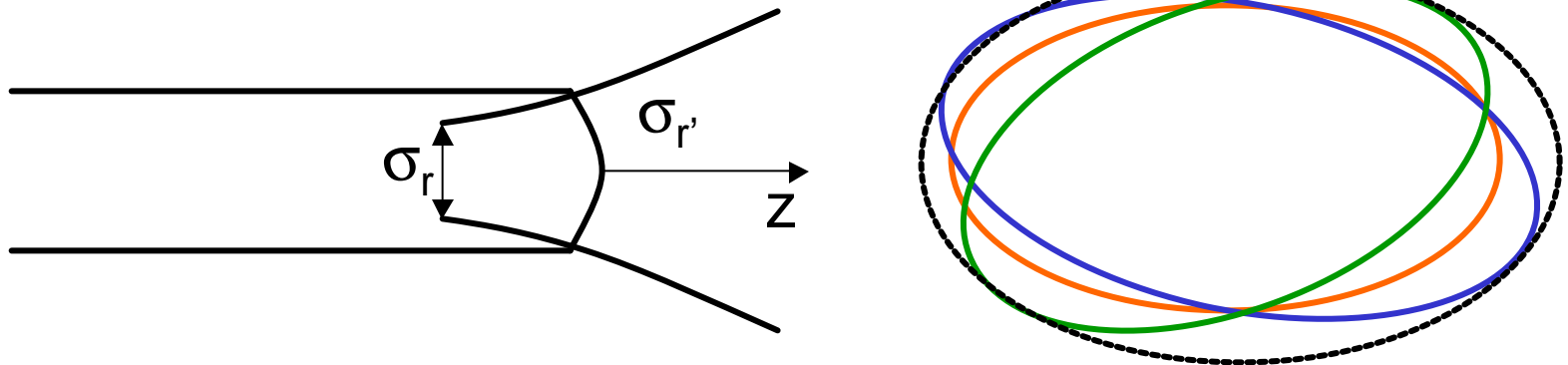
SASE intensity fluctuation (Γ distribution)

$$\frac{\Delta I}{I} = \frac{1}{\sqrt{M}}, \text{ where } M = \frac{\text{bunch length}}{\text{coherence length}}$$



Transverse and Temporal Properties: Interplay

- Transverse coherence somewhat affected by “large” SASE bandwidth (Saldin et al.)
- A different fundamental mode at each wavelength
- Smearing of radiation transverse phase space ellipses



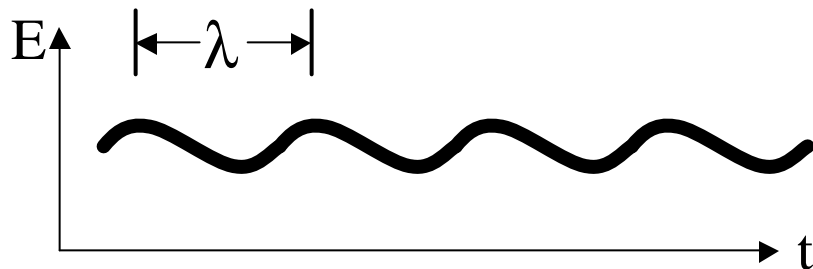
Transverse coherence: LEUTL ~ 90%, LCLS ~ 97%



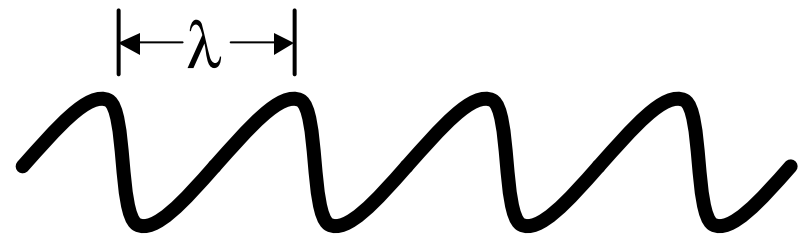
Nonlinear Harmonic Generation

- FEL instability creates energy and density modulation at λ ,
- Near saturation, strong bunching at fundamental produces rich harmonic components

small signal, linear regime



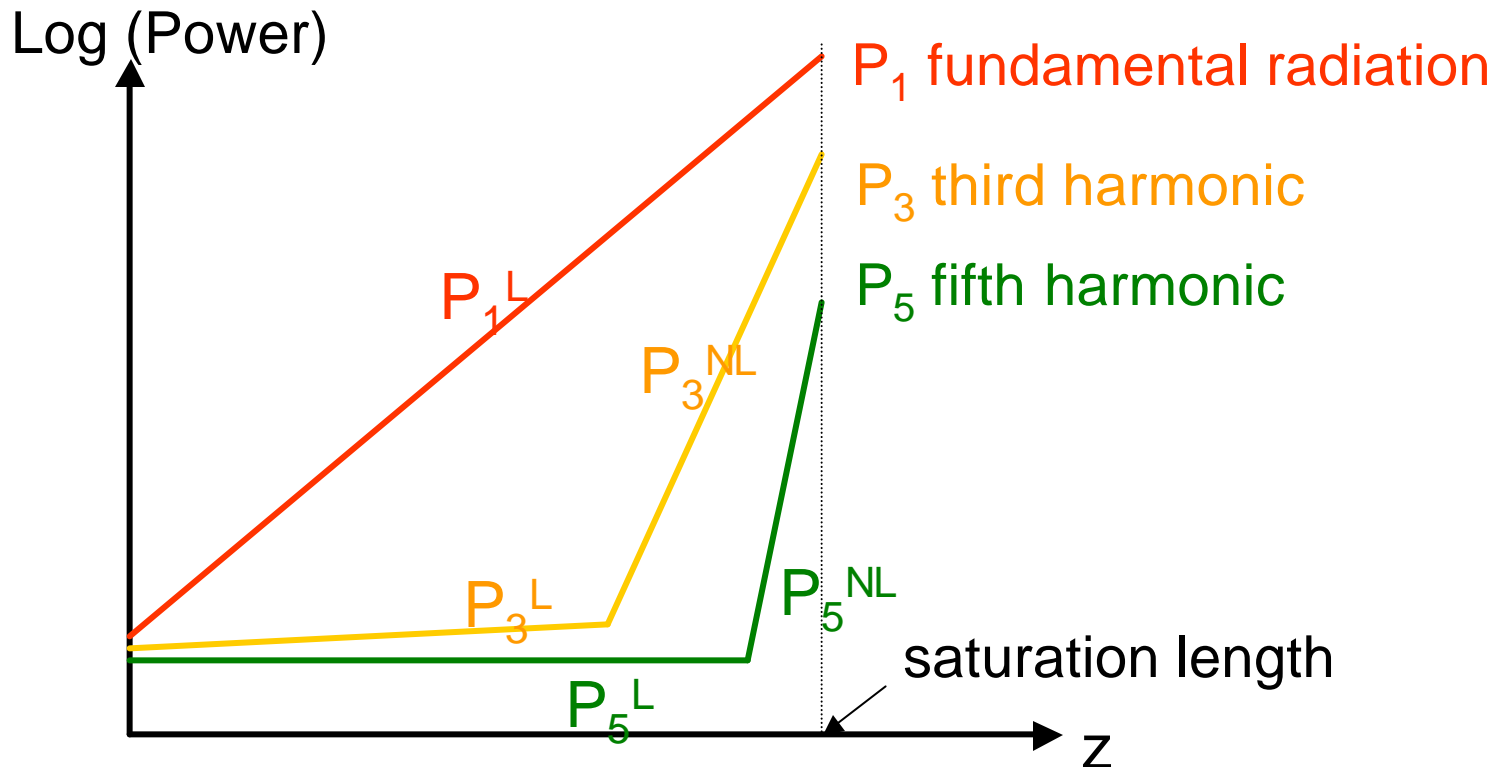
near saturation, nonlinear regime



- Coherent harmonics determined by fundamental
 - gain length L_G/n
 - transverse coherence
 - temporal structures



Plenty of Power at (3X) Shorter Wavelength

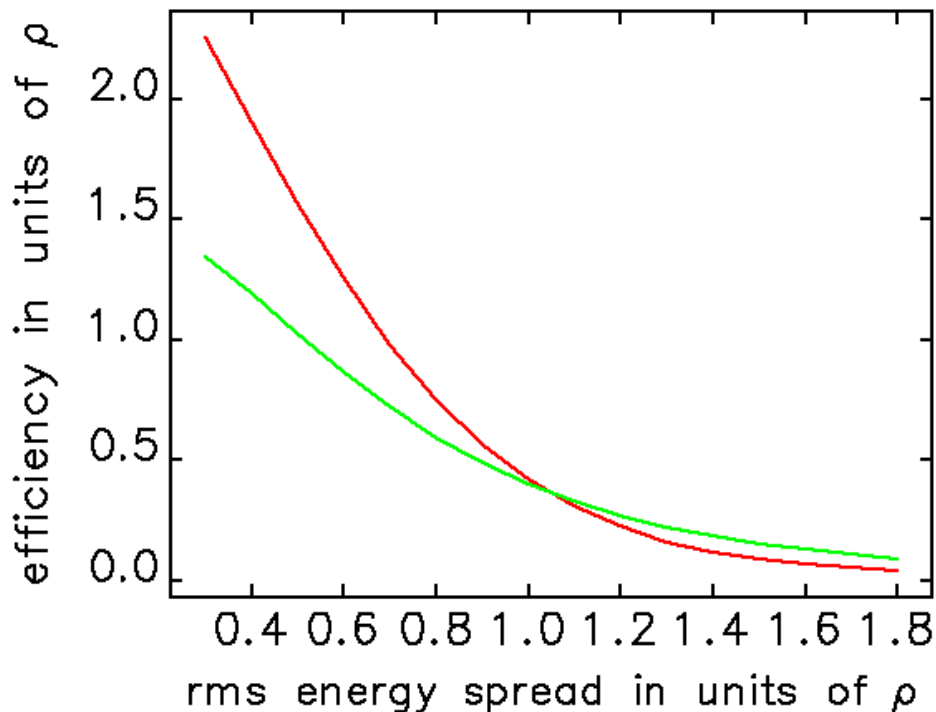


- Theory predicts third harmonic reaches 1% of fundamental, verified by recent high-gain experiments (HGHG and VISA)



Saturation Mechanism

- Quasi-linear relaxation: strong radiation field modifies e-beam distribution → increases energy spread → stops the gain → FEL saturation



- Quasi-linear solution
- Simulation fitting (Xie)

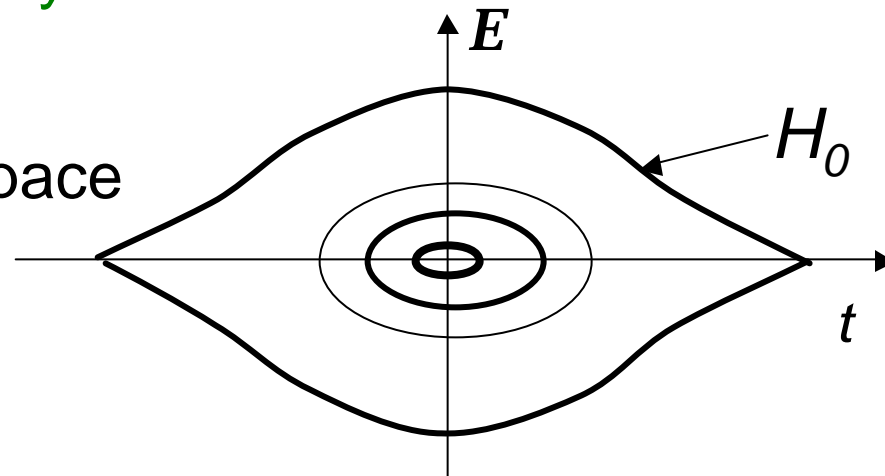


Saturation Behaviors

- XFELs operate in saturation for max. power/stability, seeding schemes go deep saturation to reduce fluctuation
- Electrons trapped by combined radiation+undulator fields

saturation phase space

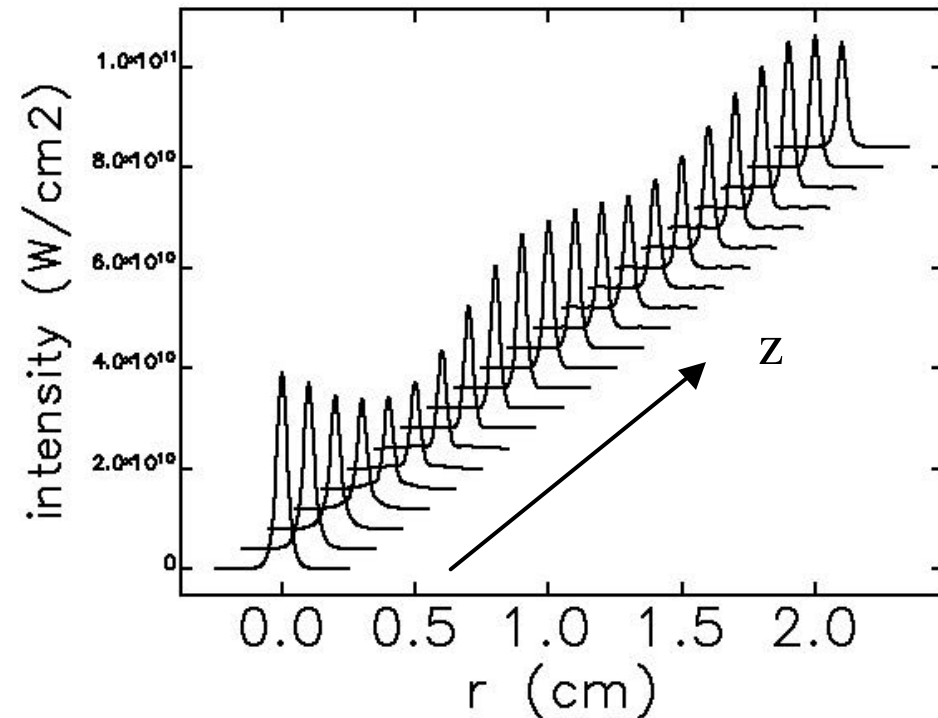
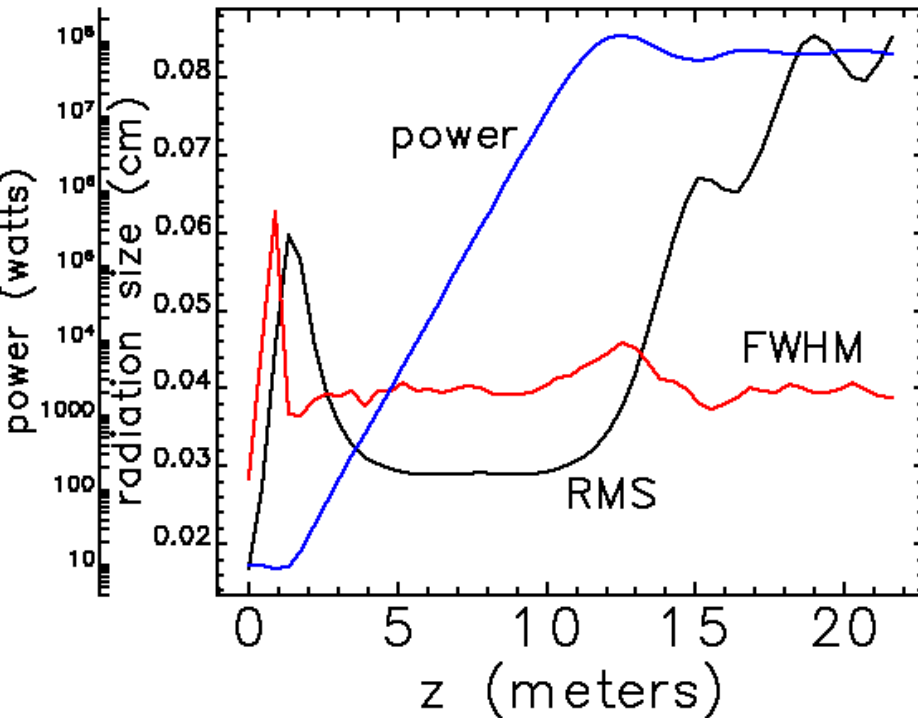
like an RF bucket



- Radiation power stays roughly constant, but phase advances due to the beam-radiation interaction
→ an effective index of refraction (>1) (Scharleman et al.)



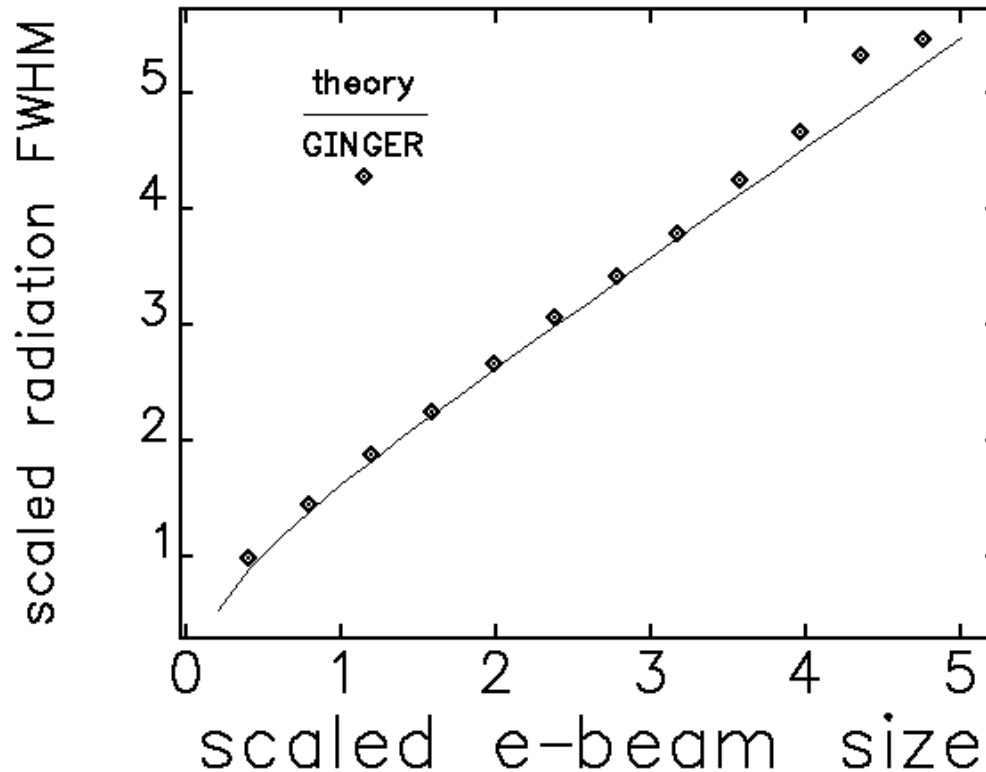
Refractive Guiding



- **Guided mode that carries fixed power \rightarrow constant FWHM**
some excess power diffracts out \rightarrow increased rms size
other excess power stays oscillatory



Guided Mode after Saturation



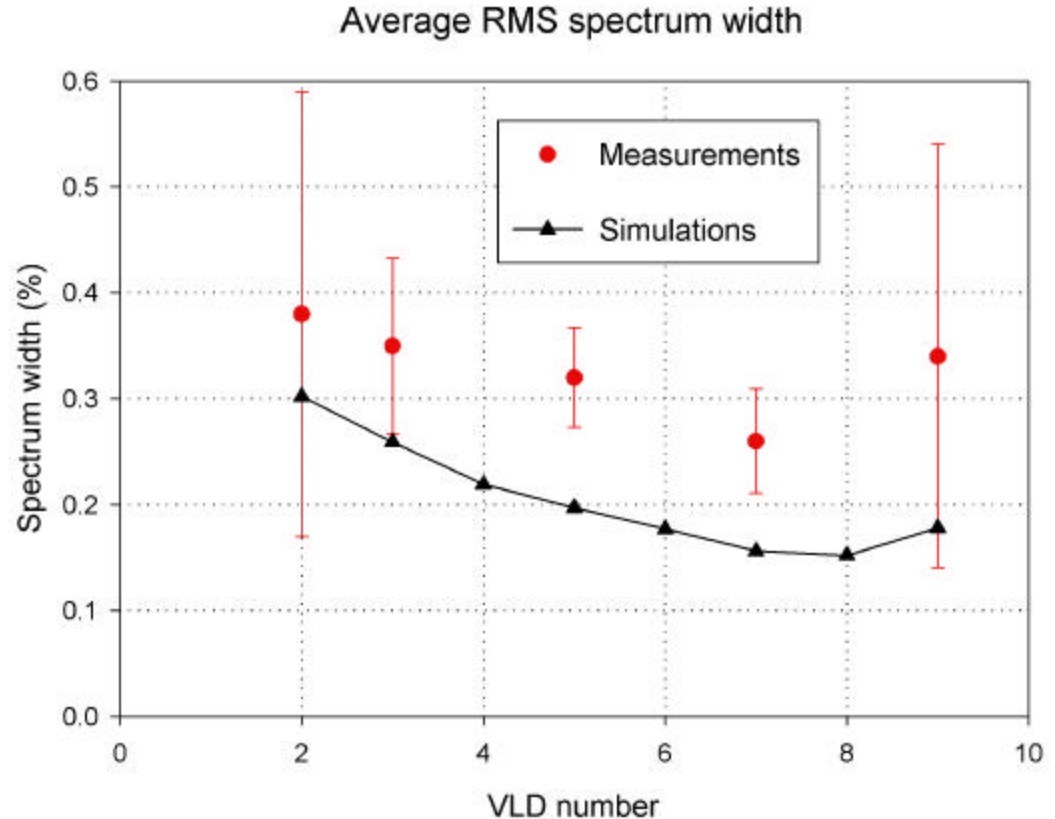
- Valid when emittance $< \lambda/4\pi$
- For XFELs, emittance $> \lambda/4\pi$, any guiding?



Sideband Instability

- Before saturation, SASE spectrum undergoes gain narrowing
- After saturation, spectrum redshifts and broadens because electron's synchrotron motion in the bucket generates sidebands

- LEUTL shows such a behavior (Sajaev et al.)





Conclusion

- The excitement of XFELs leads to progress in all areas of high-gain FEL research (including theory)
- Evolution of FEL fundamental and harmonic radiation can be completely determined for simple e-beam distributions from start-up to near saturation
- Partial understanding of saturation behavior, more needed in combination with numerical simulations
- Quantum effects (Schroeder et al.) are negligible in XFELs except for quantum fluctuation due to spontaneous radiation (Saldin et al.)